



## Misallocation or Mismeasurement?☆

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## ABSTRACT

The ratio of revenue to inputs differs greatly across plants within countries such as the U.S. and India. Such gaps may reflect misallocation which lowers aggregate productivity. But differences in measured average products need not reflect differences in true marginal products. We propose a way to estimate the gaps in true marginal products in the presence of measurement error. Our method exploits how revenue growth is less sensitive to input growth when a plant's average products are overstated by measurement error. For Indian manufacturing from 1985 to 2013, our correction lowers potential gains from reallocation by 20%. For the U.S. the effect is even more dramatic, reducing potential gains by 60% and eliminating 2/3 of a severe downward trend in allocative efficiency over 1978 to 2013.

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## 1. Introduction

The ratio of revenue to inputs differs substantially across establishments and firm within narrow industries in the U.S. and other countries (Syverson, 2011). One interpretation of such gaps is that they reflect differences in the value of marginal products for capital, labor, and intermediate inputs – misallocation with negative consequences for aggregate productivity. This point has been driven home by Restuccia and Rogerson (2008) and Hsieh and Klenow (2009). See Hopenhayn (2014) and Restuccia and Rogerson (2017) for surveys of the growing literature surrounding this topic.

Differences in measured average products need not imply differences in true marginal products. First, marginal products are proportional to average products only under Cobb-Douglas production. Second, measured differences in revenue over inputs could simply reflect poor measurement. This could stem from omitted or double-counted revenue or inputs from different divisions or products within the firm, such as in relation to headquarters. Moreover, there could be transitory mismeasurement from classifying some revenue or inputs in an adjacent year to when it actually occurred.<sup>1</sup>

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<sup>1</sup> See White et al. (2018) for how the U.S. Census Bureau tries to correct for measurement errors in its survey data on manufacturing plants. Rotemberg and White (2020) argue that the use of imputation in the U.S. but (perhaps) not in India could account for why allocative efficiency seems higher in the U.S. than in India. Bartelsman et al. (2013) and Asker et al. (2014) discuss why revenue productivity need not reflect misallocation even aside from measurement error, due to overhead costs and adjustment costs, respectively.

We propose and implement a method to quantify the extent to which measured average products reflect true marginal products in the presence of measurement error. Our method is able to detect measurement error in revenue and inputs which is additive but whose variance can scale up with the plant's true revenue and inputs. Omitted revenue or inputs from products could take this form, for example, if the revenue from a firm's different products is not well correlated. Our method cannot identify proportional measurement error, and therefore may yield a lower bound on the magnitude of measurement error.

The intuition for our method is as follows. Imagine a world with constant (proportional) differences in true marginal products. The only shocks are to idiosyncratic plant productivity. Productivity shocks will move true revenue and inputs around across plants in the same proportion.<sup>2</sup> Thus, in the absence of measurement error, revenue growth will be proportional to input growth across all plants. Now suppose, instead, that revenue is overstated for a given plant. If this measurement error is additive and fixed over time, then the plant's measured revenue will move by less in percentage terms in response to a change in its productivity. Similarly, if a plant has overstated inputs in an additive and fixed way, its measured inputs will move less than proportionately in response to productivity shocks. Thus, if a plant's revenue/inputs are overstated by measurement error, its measured revenue growth will be less responsive to its measured input growth. We can then gauge the importance of measurement error in the cross-section by the degree to which high average product plants exhibit a low elasticity of revenue growth with respect to input growth.

Our method applies to less stark environments with changing true marginal products and measurement error over time for plants. A key restriction we do require is that the measurement errors be orthogonal to the true marginal products. Our approach involves regressing revenue growth on input growth within deciles of plants in terms of their average products. The extent to which the coefficients decrease with the decile (level) of TFPR speak to how much measurement error is contributing to the dispersion in measured average products in the cross-section.

We apply our method to panel data on manufacturing plants in the U.S. (1978–2013) and India (1985–2013). We examine about 50,000 plants per year in the U.S. Annual Survey of Manufacturers (ASM) from the Longitudinal Research Database (LRD). In India we look at about 43,000 plants per year from their Annual Survey of Industries (ASI).

We first report estimates of allocative efficiency without correcting for measurement error. The U.S. exhibits a severe decline, seemingly going from producing 3/5 as much as it could by equalizing marginal products across plants to producing only 1/3 as much as it could. If true, this plunge reduced the annual TFP growth rate by 1.7 percent per year over 1978–2013. By comparison, we estimate that Indian manufacturing operated at about 1/2 efficiency, with a fair bit of volatility from year to year but no clear trend despite major policy reforms. Thus by the end of the sample the U.S. appears to have lower allocative efficiency than India.

Once we correct for measurement error, U.S. allocative efficiency is much higher (above 2/3) with a modest downward trend and much less volatility. Measurement error appears to be a growing problem in Census LRD plant data. In the Indian ASI, correcting for measurement error has a less dramatic effect. As a result, corrected allocative efficiency appears consistently higher in the U.S., raising manufacturing productivity by 10 to 50 percent relative to that in India (in all but one year).

Our results imply that sluggish TFP growth in U.S. manufacturing in recent decades does not seem to be driven by declining allocative efficiency. One must look elsewhere for explanations, such as falling innovation rates. To the extent that slow growth has contributed to low risk-free real interest rates, a corollary of our findings is that such returns do not appear to be low because of low allocative efficiency, at least in manufacturing.

The rest of the paper proceeds as follows. [Section 2](#) presents a simple model wherein both measurement error and distortions are fixed over time. [Section 3](#) presents the full model, which allows both measurement error and distortions to change over time. [Section 4](#) describes the U.S. and Indian datasets, and raw allocative efficiency patterns in the absence of our correction for measurement error. [Section 5](#) lays out our method for quantifying measurement error, and applies it to the panel data on manufacturing plants in the U.S. and India. As stated, these estimates impose the strong assumption that measurement error and true productivity are uncorrelated. We also rely on local approximations, so in [Section 6](#) we examine how well our measure performs under alternative assumptions on the properties of shocks to productivity, distortions, and measurement error. [Section 7](#) shows how correcting for measurement error affects the picture of allocative efficiency in the U.S. and India.

## 2. An illustrative model

In order to convey intuition for our methodology, we first present a simple model. We assume the economy has a fixed number of workers  $L$  and a single, competitive final goods sector producing aggregate output  $Y$ . Aggregate output is, in turn,

<sup>2</sup> Output increases more than inputs in response to a productivity shock, of course. But a plant's relative output price will decline with productivity so that its revenue will rise by the same proportion as its inputs. This is true if the plant's price-cost markup, or true ratio of revenue to inputs, does not change with its productivity.

produced by CES aggregation of the output  $Y_i$  of  $N$  intermediate goods producers with elasticity of substitution  $\epsilon$ :

$$Y = \left( \sum_{i=1}^N Y_i^{1-\frac{1}{\epsilon}} \right)^{\frac{1}{1-\frac{1}{\epsilon}}} . \quad (1)$$

The price index of the final good is given by  $P = (\sum_i P_i^{1-\epsilon})^{\frac{1}{1-\epsilon}}$  and is normalized to 1. Intermediate firms produce output using a linear production technology in labor under heterogeneous productivities:  $Y_i = A_i L_i$ . These firms are monopolistically competitive and face a downward sloping demand curve:  $Y_i \propto P_i^{-\epsilon}$ . They maximize profits taking as given  $Y$ ,  $P$ , the wage  $w$ , and an idiosyncratic revenue distortion  $\tau_i$ :

$$\Pi_i = \frac{1}{\tau_i} P_i Y_i - w L_i . \quad (2)$$

The researcher observes only *measured* revenue  $\widehat{P_i Y_i} \equiv P_i Y_i + g_i$  and *measured* labor  $\widehat{L_i} \equiv L_i + f_i$ . Given the assumed CES demand structure, firms charge a common markup over their marginal cost (gross of the distortion):

$$P_i = \left( \frac{\epsilon}{\epsilon - 1} \right) \times \left( \tau_i \cdot \frac{w}{A_i} \right) . \quad (3)$$

True revenue is therefore proportional to the product of true labor times and the idiosyncratic distortion:

$$P_i Y_i \propto \tau_i \cdot L_i . \quad (4)$$

Thus variation across firms in true average revenue products  $\left( \frac{P_i Y_i}{L_i} \right)$  is solely due to the distortion. Variation in *measured* average revenue products (TFPR), however, reflects both the distortion and measurement errors:

$$\text{TFPR}_i \equiv \frac{\widehat{P_i Y_i}}{\widehat{L_i}} \propto \left[ \tau_i \times \frac{1 + g_i / (P_i Y_i)}{1 + f_i / L_i} \right] . \quad (5)$$

Our methodology will allow both the true distortions and the measurement errors to vary over time. But to convey intuition, we make a number of simplifying assumptions in this section:

1. The true distortions  $\tau_i$  are fixed over time
2. The additive measurement error terms  $g_i$  and  $f_i$  are fixed over time
3. The idiosyncratic productivities  $A_{it}$  are time-varying

Under these assumptions,

$$\Delta P_i Y_i = \Delta L_i = (\epsilon - 1) \Delta A_i . \quad (6)$$

Thus true revenue growth equals true input growth for a given plant. Therefore, regressing revenue growth on input growth should yield a coefficient of 1 independently of a plant's level of TFPR.

In the presence of measurement error, however, the relation between measured revenue and input growth in this economy is, for small  $\Delta A_i$ ,

$$\Delta \widehat{P_i Y_i} = \Delta \widehat{L_i} \cdot \frac{\tau_i}{\text{TFPR}_i} . \quad (7)$$

The higher is TFPR relative to the true distortion  $\tau$ , the lower is revenue growth relative to input growth. To the extent measurement errors, not true distortions, drive TFPR differences, the estimated elasticity of plant revenue growth on input growth will be predictably lower for plants with higher TFPR.

In [Section 5](#) we will generalize this logic to allow for shocks to both measurement error and distortions. The intuition from this simple example will remain: the extent to which high TFPR plants exhibit a low elasticity of revenue with respect to inputs will help us to estimate the role of measurement error in TFPR dispersion.<sup>3</sup> We will use this, in turn, to estimate the variance of the true distortion and therefore the true level of allocative efficiency. In the next section we present the full model and a decomposition of aggregate and sectoral TFP into allocative efficiency vs. other terms.

### 3. Model

We now generalize our illustrative model to allow for capital and for multiple sectors. We show how aggregate TFP reflects cross-sector distortions as well as the individual sectors' TFPs, then how each sector's TFP reflects its particular set of distortions.

<sup>3</sup> In an earlier version of this paper, we used a regression equation close to (7), specifically, we regressed revenue growth on input growth, TFPR, and the interaction of input growth and TFPR across plants. The coefficient on the interaction term provided direct information on the extent of TFPR dispersion due to measurement error. This approach works well except in cases where measurement error is a large fraction of all TFPR dispersion, but is still a useful diagnostic.

### 3.1. Economic environment

We consider an economy with  $S$  sectors,  $L$  workers and an exogenous capital stock  $K$ . There are an exogenous number of firms  $N_s$  operating in each sector. A representative firm produces a single final good  $Q$  in a perfectly competitive final output market. This final good is produced using gross output  $Q_s$  from each sector  $s$  with a Cobb-Douglas production technology:

$$Q = \prod_{s=1}^S Q_s^{\theta_s} \text{ where } \sum_{s=1}^S \theta_s = 1. \quad (8)$$

We normalize  $P$ , the price of the final good, to 1. The final good can either be consumed or used as an intermediate input:

$$Q = C + X. \quad (9)$$

All firms use the same intermediate input, with the amounts denoted  $X_{si}$  so that  $X \equiv \sum_{s=1}^S X_s = \sum_{s=1}^S \sum_{i=1}^{N_s} X_{si}$ .

Sectoral output  $Q_s$  is a CES aggregate of the outputs of the  $N_s$  sector- $s$  firms:

$$Q_s = \left( \sum_{i=1}^{N_s} Q_{si}^{1-\frac{1}{\epsilon}} \right)^{\frac{1}{1-\frac{1}{\epsilon}}}. \quad (10)$$

We denote by  $P_s$  the price index of output from sector  $s$ . Firms have idiosyncratic productivity draws  $A_{si}$ , and produce output  $Q_{si}$  using a Cobb-Douglas technology in capital, labor and intermediate inputs:

$$Q_{si} = A_{si} (K_{si}^{\alpha_s} L_{si}^{1-\alpha_s})^{\gamma_s} X_{si}^{1-\gamma_s} \text{ where } 0 < \alpha_s, \gamma_s < 1. \quad (11)$$

The output elasticities  $\alpha_s$  and  $\gamma_s$  are sector-specific, but time-invariant and common across firms within a sector. Firms are monopolistically competitive and face a downward sloping demand curve given by  $Q_{si} = Q_s \left( \frac{P_{si}}{P_s} \right)^{-\epsilon}$ . Firms treat  $P_s$  and  $Q_s$  as exogenous. Firms also face idiosyncratic labor distortions  $\tau_{si}^L$ , capital distortions  $\tau_{si}^K$  and intermediate input distortions  $\tau_{si}^X$ . They maximize profits  $\Pi_{si}$  taking input prices as given.

$$\Pi_{si} = R_{si} - (1 + \tau_{si}^L) w L_{si} - (1 + \tau_{si}^K) r K_{si} - (1 + \tau_{si}^X) P X_{si}, \quad (12)$$

where  $R_{si} \equiv P_{si} Q_{si}$  is firm revenue.

### 3.2. Aggregate TFP

We define aggregate TFP as aggregate real consumption (or equivalently value-added) divided by an appropriately weighted Cobb-Douglas bundle of aggregate capital and labor:

$$TFP \equiv \frac{C}{L^{1-\tilde{\alpha}} K^{\tilde{\alpha}}} \quad \text{where} \quad \tilde{\alpha} \equiv \frac{\sum_{s=1}^S \alpha_s \gamma_s \theta_s}{\sum_{s=1}^S \gamma_s \theta_s}. \quad (13)$$

We show in our [Online Appendix](#) that

$$TFP = \bar{T} \times \prod_{s=1}^S TFP_s^{\frac{\theta_s}{\sum_{s=1}^S \gamma_s \theta_s}}. \quad (14)$$

$\bar{T}$  captures the effect of the *sectoral* distortions  $\tau_s^L$ ,  $\tau_s^K$  and  $\tau_s^X$ , which are the revenue-weighted harmonic means of the idiosyncratic firm-level distortions.<sup>4</sup> Sectoral TFP is then:

$$TFP_s \equiv \frac{Q_s}{(K_s^{\alpha_s} L_s^{1-\alpha_s})^{\gamma_s} X_s^{1-\gamma_s}}. \quad (15)$$

*Within-sector* misallocation lowers  $TFP_s$ . Meanwhile, sectoral distortions will induce a *cross-sector* misallocation of resources which will show up in  $\bar{T}$ . While cross-sector misallocation is of interest, it is not the focus of this paper. We therefore leave it to future research to determine how important this could be in determining cross-country aggregate TFP gaps.

### 3.3. Sectoral TFP decomposition

Sector-level TFP is a function of firm-level productivities and distortions:

$$TFP_s = \left[ \sum_{i=1}^{N_s} A_{si}^{\epsilon-1} \left( \frac{\tau_{si}}{\tau_s} \right)^{1-\epsilon} \right]^{\frac{1}{\epsilon-1}}, \quad (16)$$

<sup>4</sup>  $(1 + \tau_s^L) \equiv \left[ \sum_{i=1}^{N_s} \frac{R_{si}}{R_s} \frac{1}{1 + \tau_{si}^L} \right]^{-1}$  and similarly for  $(1 + \tau_s^K)$  and  $(1 + \tau_s^X)$ . The [Online Appendix](#) expresses sectoral distortions as a function only of firm distortions and productivities.

$$\text{where } \tau_{si} \equiv \left[ (1 + \tau_{si}^L)^{1-\alpha_s} (1 + \tau_{si}^K)^{\alpha_s} \right]^{\gamma_s} (1 + \tau_{si}^X)^{1-\gamma_s}, \quad (17)$$

$$\text{and } \tau_s \equiv \left[ (1 + \tau_s^L)^{1-\alpha_s} (1 + \tau_s^K)^{\alpha_s} \right]^{\gamma_s} (1 + \tau_s^X)^{1-\gamma_s}. \quad (18)$$

We can go one step further, and decompose sectoral TFP into the product of four terms: allocative efficiency ( $AE_s$ ), a productivity dispersion term ( $PD_s$ ), average productivity ( $\bar{A}_s$ ), and a variety term ( $N_s^{\frac{1}{\epsilon-1}}$ ).

$$TFP_s = \underbrace{\left[ \frac{1}{N_s} \sum_i \left( \frac{A_{si}}{\bar{A}_s} \right)^{\epsilon-1} \left( \frac{\tau_{si}}{\tau_s} \right)^{1-\epsilon} \right]^{\frac{1}{\epsilon-1}}}_{AE_s = \text{Allocative Efficiency}} \times \underbrace{\left[ \frac{1}{N_s} \sum_i \left( \frac{A_{si}}{\bar{A}_s} \right)^{\epsilon-1} \right]^{\frac{1}{\epsilon-1}}}_{PD_s = \text{Productivity Dispersion}} \times \underbrace{N_s^{\frac{1}{\epsilon-1}}}_{\text{Variety}} \times \underbrace{\bar{A}_s}_{\text{Ave. Productivity}}. \quad (19)$$

$\bar{A}$  is the power mean of idiosyncratic productivities,  $\left[ \frac{1}{N_s} \sum_{i=1}^{N_s} (A_{si})^{\epsilon-1} \right]^{\frac{1}{\epsilon-1}}$ , and  $\bar{A}$  is the geometric mean of idiosyncratic productivities  $\prod_{i=1}^{N_s} A_{si}^{\frac{1}{N_s}}$ .  $AE_s$  is maximized and equal to 1 when there is no variation in the distortions across firms ( $\tau_{si} = \tau_s \forall i$ ). The productivity dispersion term ( $PD_s$ ) is the ratio of the power mean to the geometric mean. Because  $\epsilon > 1$ , greater dispersion in firm-level productivities induces a reallocation of labor towards the most productive firms, thereby increasing sectoral TFP.  $N_s^{\frac{1}{\epsilon-1}}$  captures the productivity gains from expanding the set of varieties available to sectoral goods producers. Finally, it is clear why increases in average productivity ( $\bar{A}_s$ ) should increase sectoral TFP.

#### 4. Inferring Allocative Efficiency

Our goal is to present a methodology for inferring allocative efficiency ( $AE_s$ ) from plant-level data while allowing for measurement error. In this section we briefly describe the U.S. and Indian datasets we use, present the model-based approach to inferring allocative efficiency in the *absence* of measurement error, and show raw allocative efficiency patterns in the data.

##### 4.1. Datasets

We use two datasets of manufacturing plants in this paper: the Indian Annual Survey of Industries (ASI) from 1985 to 2013 and the U.S. Longitudinal Research Database (LRD) from 1978 to 2013. We look at plants rather than firms for two reasons. First, the Indian data only provides information on plants, not firms. Second, the U.S. and India results in [Hsieh and Klenow \(2009\)](#) are a key point of comparison, and these are done at the plant level. See [Giroud et al. \(2018\)](#) and [Kehrig and Vincent \(2020\)](#) for evidence on revenue productivity dispersion across plants within firms.

The ASI is a nationally representative survey of formal manufacturing plants in India. The coverage includes plants with at least 10 workers using power, and plants with at least 20 workers not using power. Plants fall into two categories: *Census* and *Sample*. *Census* plants are surveyed every year, and consist of plants with at least 100 workers (the threshold increases to 200 workers in some survey years) as well as all plants in 12 of the “industrially backwards” states. *Sample* plants are randomly sampled each year within state  $\times$  industry cells. Official panel identifiers are available from 1998 on, and we use panel identifiers from an old version of the publicly available ASI prior to 1998. We construct an industry classification consisting of 50 manufacturing industries which are consistently defined throughout our time period.<sup>5</sup>

The LRD is a database of U.S. manufacturing plants put together by the U.S. Census Bureau. The coverage is all manufacturing plants with at least one employee. The database includes information from the Annual Survey of Manufactures (ASM) and the Census of Manufactures (CMF), augmented with establishment identifiers from the Longitudinal Business Database (LBD). The CMF is a census which is conducted in years ending in 2 or 7. The ASM is a survey which is conducted in all other years. The ASM covers large plants with certainty (typically plants with at least 100 workers, though the threshold varies by survey year) and randomly samples smaller plants. The ASM sample is redrawn in years ending in 4 and 9. In order to avoid any large changes in sample size over time, we use only the ‘ASM’ sample plants in CMF years. From here on, we refer to our U.S. dataset as the LRD. We use the harmonized sectoral classification from [Fort and Klimek \(2016\)](#) at the NAICS 3-digit level (86 sectors).

The main variables we use are gross output, labor costs, capital, inventories, and intermediate inputs. We construct gross output as the sum of shipments, changes in finished and semi-finished good inventories, and other revenues. We construct intermediate inputs as the sum of materials, fuels and other expenditures. We include unpaid family workers in our measure of labor in India. We construct labor costs as the sum of wages, salaries, bonuses and supplemental labor costs. We set

<sup>5</sup> The official sectoral classification (NIC) changed in 1987, 1998, 2004 and 2008. We use official NIC concordances to construct our harmonized classification.

the capital stock as the sum of fixed assets and the stock of inventories.<sup>6</sup> Official sampling weights are used in all of our calculations. We discuss more details about variable construction in our [Online Appendix](#).

We clean the ASI and LRD using the same approach. We drop plants with missing or negative values for any of the variables described above. We then trim the 1% tails of TFPR and TFPQ deviations from the industry average in each year (TFPR and TFPQ are defined in the next section). We describe these steps in more detail in our [Online Appendix](#). Our final sample sizes are 1,806,000 plant-years for the U.S. and 943,186 plant-years for India.<sup>7</sup>

#### 4.2. Inferring allocative efficiency

Continuing to use  $\sim$ 's to denote *measured* values, TFPR and TFPQ are:

$$\text{TFPR}_{si} \equiv \frac{\hat{R}_{si}}{(\hat{K}_{si}^{\alpha_s} \hat{L}_{si}^{1-\alpha_s})^{\gamma_s} \hat{X}_{si}^{1-\gamma_s}}, \quad (20)$$

$$\text{TFPQ}_{si} \equiv \frac{(\hat{R}_{si})^{\frac{\epsilon}{\epsilon-1}}}{(\hat{K}_{si}^{\alpha_s} \hat{L}_{si}^{1-\alpha_s})^{\gamma_s} \hat{X}_{si}^{1-\gamma_s}}. \quad (21)$$

In the absence of measurement error, TFPR would be proportional to the distortion and TFPQ would be proportional to productivity:

$$\frac{R_{si}}{(\hat{K}_{si}^{\alpha_s} \hat{L}_{si}^{1-\alpha_s})^{\gamma_s} \hat{X}_{si}^{1-\gamma_s}} \propto \tau_{si} \quad \text{and} \quad \frac{(R_{si})^{\frac{\epsilon}{\epsilon-1}}}{(\hat{K}_{si}^{\alpha_s} \hat{L}_{si}^{1-\alpha_s})^{\gamma_s} \hat{X}_{si}^{1-\gamma_s}} \propto A_{si}. \quad (22)$$

We infer sectoral allocative efficiency using the following expression:

$$\widehat{AE}_s = \left[ \sum_{i=1}^{N_s} \left( \frac{\text{TFPQ}_{si}}{\text{TFPQ}_s} \right)^{\epsilon-1} \left( \frac{\text{TFPR}_{si}}{\text{TFPR}_s} \right)^{1-\epsilon} \right]^{\frac{1}{\epsilon-1}}, \quad (23)$$

$$\text{where } \text{TFPQ}_s = \left[ \sum_{i=1}^{N_s} \text{TFPQ}_{si}^{\epsilon-1} \right]^{\frac{1}{\epsilon-1}}, \quad (24)$$

$$\text{and } \text{TFPR}_s = \left( \frac{\epsilon}{\epsilon-1} \right) \left[ \frac{\text{MRPL}_s}{(1-\alpha_s)\gamma_s} \right]^{(1-\alpha_s)\gamma_s} \left[ \frac{\text{MRPK}_s}{\alpha_s\gamma_s} \right]^{\alpha_s\gamma_s} \left[ \frac{\text{MRPX}_s}{1-\gamma_s} \right]^{1-\gamma_s}. \quad (25)$$

MRPL<sub>s</sub>, MRPK<sub>s</sub> and MRPX<sub>s</sub> are the revenue-weighted harmonic mean values of the marginal products of labor, capital and intermediates, respectively. E.g.,

$$\text{MRPK}_s = \left[ \sum_i \frac{\hat{R}_{si}}{\hat{R}_s} \frac{1}{\text{MRPK}_{si}} \right]^{-1}, \quad (26)$$

$$\text{MRPK}_{si} = \left( \frac{\epsilon-1}{\epsilon} \right) \alpha_s \gamma_s \frac{\hat{R}_{si}}{\hat{K}_{si}}. \quad (27)$$

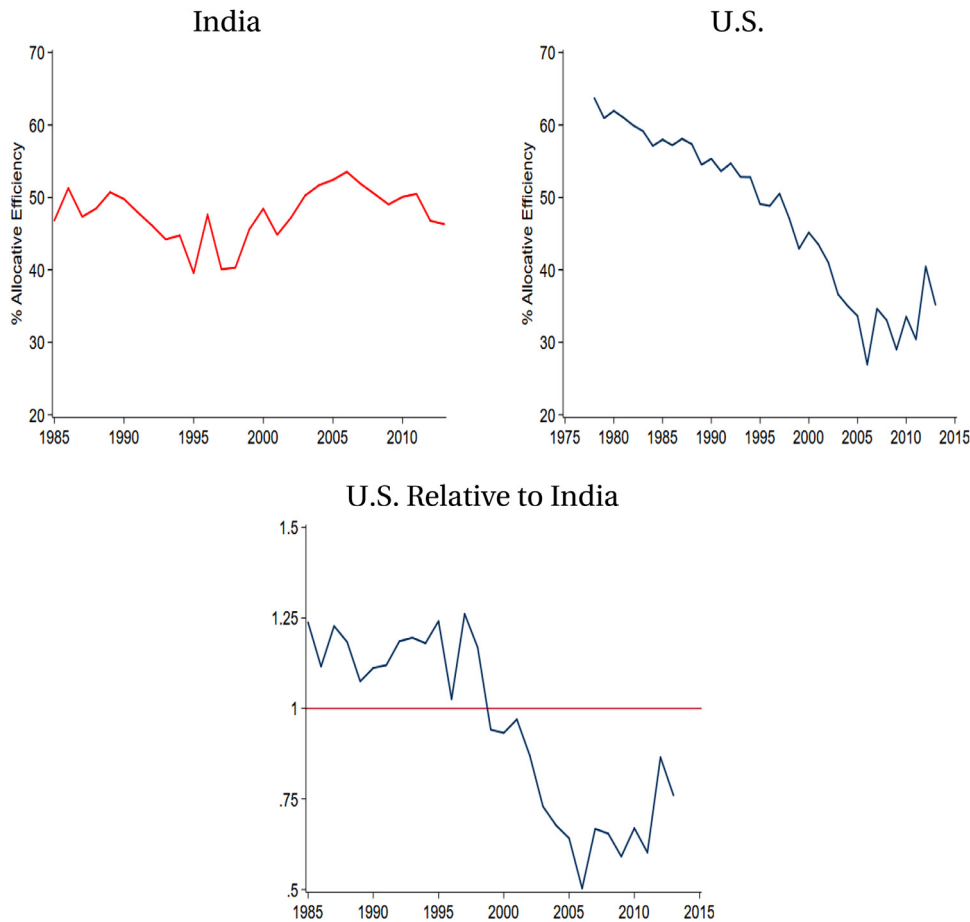
Aggregating across sectors we obtain inferred aggregate allocative efficiency, which is equal to true allocative efficiency when there is no measurement error:

$$\widehat{AE}_t = \prod_{s=1}^S \widehat{AE}_{st}^{\frac{\theta_{st}}{\sum_{s=1}^S \gamma_s \theta_{st}}}. \quad (28)$$

In order to obtain estimates of allocative efficiency over time for the U.S. and India we need to pin down a number of parameters in the model. Based on evidence from [Redding and Weinstein \(2019\)](#), we pick a value of  $\epsilon = 4$  for the elasticity of substitution across plants. Allocative *inefficiencies* are amplified under higher values of this elasticity. We infer  $\alpha_s$  and  $\gamma_s$

<sup>6</sup> Because of data availability, we use the nominal book value of fixed assets in India, and the real market value of fixed assets in the U.S. Book value capital stocks are not reported every year in the U.S., unlike investment in fixed assets. Our real capital stock measure is constructed using the perpetual inventory method. We do not deflate any nominal variables. Industry-level deflators would difference out because all of our analyses focus on within-industry differences across plants.

<sup>7</sup> We round U.S. observation counts in accordance with Census data disclosure rules.



**Fig. 1.** Allocative Efficiency in India and the U.S. *Source:* Indian ASI and U.S. LRD. The top figures show the % allocative efficiency for both countries. Average allocative efficiency is 48% in both India and the U.S. over the respective sample periods. The bottom figure plots the ratio of U.S. allocative efficiency to Indian allocative efficiency for the years 1985 to 2013 (years in which the datasets overlap).

based on country-specific average sectoral cost shares.<sup>8</sup> We allow the aggregate output shares  $\theta_{st}$  to vary across years, and base them on country-specific sectoral shares of manufacturing output.<sup>9</sup> We use labor costs as our measure of labor input because it captures variation in human capital and hours worked across plants.

#### 4.3. Time-series results

Fig. 1 plots inferred allocative efficiency for India and the U.S. over their respective samples. While allocative efficiency exhibits no clear trend in India, there is a remarkable decrease in allocative efficiency in the U.S. from 1978 to 2006. As a result, over the entire sample allocative efficiency surprisingly averages the same 48% for both India and the United States.<sup>10</sup> The bottom plot in Fig. 1 shows the ratio of U.S. to Indian allocative efficiency for their overlapping samples. Allocative efficiency is *lower* in the U.S. than in India by around the year 2000 — substantially lower, as U.S. allocative efficiency averages only two-thirds of Indian allocative efficiency from 2003 to 2013.

The dramatic decline in allocative efficiency for the U.S. mirrors a sharp rise in its TFPR dispersion. Fig. 2 displays the variance of  $\ln(\text{TFPR})$  for both India and the U.S. for 1985 to 2013.<sup>11</sup> While the Indian data display little or no trend, the

<sup>8</sup> We assume a rental rate for fixed assets of 20% and a rental rate of 10% for inventories.

<sup>9</sup> Our results are not sensitive to the choice of constant or time-varying sectoral shares.

<sup>10</sup> Average gains from full reallocation are 123% for the U.S. versus 111% for India. In contrast, Hsieh and Klenow (2009) found 40–60% higher potential gains from reallocation in India than in the United States. Our estimates diverge from Hsieh and Klenow's for several reasons: We use gross output while they use value added; we have a 1978–2013 LRD sample while they have 1987, 1992, and 1997 Census plants; we trim 1% tails in the U.S., while they trim 2%. (They inconsistently trimmed 2% for the U.S. and only 1% for India.)

<sup>11</sup> Fig. 2 plots the variance of  $\ln(\text{TFPR})$  weighting plants by output shares. This measure maps more directly into allocative efficiency than the unweighted variance. The unweighted variance of  $\ln(\text{TFPR})$  exhibits the same trend in the U.S., with the variance increasing from 0.06 in 1978 to 0.16 in 2009, before falling slightly to 0.13 in 2013.



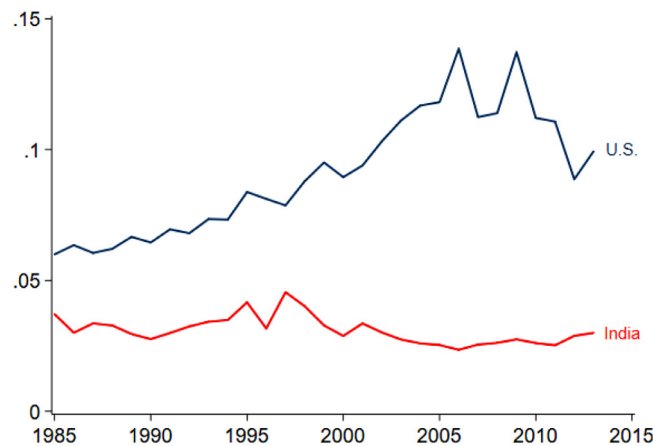


Fig. 2. Variance of  $\ln(\text{TFPR})$  Source: Indian ASI and U.S. LRD. The variance of  $\ln(\text{TFPR})$  is weighted by gross output.

variance of  $\ln(\text{TFPR})$  essentially doubles for the U.S. from 1985 to the late 2000s, before retreating part way by the end of the sample. [Online Appendix](#) Figure A2 plots the 90:50 and 50:10 percentile ratios of  $\ln(\text{TFPR})$  for the U.S., and shows that the increasing variance is mostly coming from the right tail.

As noted, allocative efficiency averaged 48% in both the Indian and U.S. samples. This may seem inconsistent with the markedly higher TFPR dispersion for the U.S. displayed in [Fig. 2](#). But India's intermediate share is 82.2% while the U.S. intermediate share is 65.3%, and this higher intermediate share magnifies the impact of distortions on allocative efficiency. A related point, point is that TFPR dispersion tends to be smaller when working with gross output than with value added; see [Gandhi et al. \(2017\)](#) for example.

[Decker et al. \(2020\)](#) document that dispersion in labor productivity increased both in the Annual Survey of Manufactures and in the Revenue-Enhanced Longitudinal Business Database, suggesting some true increase in productivity dispersion. The increase in TFPR dispersion we document in the ASM is much larger than they find in labor productivity. If the rising dispersion in TFPR we find is true, it would have far more dramatic implications for allocative efficiency.<sup>12</sup> In [Section 7](#) we examine how correcting for measurement error alters these patterns, in addition to its impact on trends in allocative efficiency.

Figure A3 in the [Online Appendix](#) shows that TFPQ dispersion rose in both the U.S. and India from 1985–2013. The variance in logs rose from about 0.35 to 0.45 or more in both countries. At the same time, the elasticity of TFPR with respect to TFPQ rose in the U.S. and fell in India – see Figure A4 in the [Online Appendix](#). The elasticity rose from around 0.27 to 0.37 in the U.S. over time. According to some theories, such as [Bento and Restuccia \(2017\)](#), this elasticity can have important implications for incentives to invest in TFPQ improvements.

In the next section we present our methodology to correct TFPR for measurement errors with the goal of obtaining measures of allocative efficiency that are more robust to such errors.

## 5. Measurement error

Calculations of misallocation, including those just presented, interpret plant differences in measured average revenue products (TFPR) as differences in true marginal products. In many of these studies the underlying plant data are longitudinal. We will show that, using such data, one can project the elasticity of revenue with respect to inputs on TFPR to answer the question: to what extent do plants with higher measured average products have higher true marginal products? The logic is similar to using the covariance of two noisy measures of a variable, here noisy measures of a plant's marginal revenue product, to recover a truer measure of the variable.

### 5.1. Measurement error and TFPR

Consider the following description of measured inputs  $\hat{I}$  and measured revenue  $\hat{R}$  for plant  $i$  (year subscripts implicit):

$$\hat{I}_i \equiv \phi_i \cdot I_i + f_i, \quad (29)$$

$$\hat{R}_i \equiv \chi_i \cdot R_i + g_i, \quad (30)$$

<sup>12</sup> The variance of labor productivity in [Decker et al. \(2020\)](#) increases by roughly 20–30% between 1996 and 2012. However, the variance of  $\ln(\text{TFPR})$  in [Fig. 2](#) increases by roughly 40–60% between 1996 and the late 2000s.



where  $I$  and  $R$  denote true inputs and revenues,  $f$  and  $g$  reflect additive measurement errors, and  $\phi$  and  $\chi$  are multiplicative errors. Note that the additive terms  $f$  and  $g$  could alternatively reflect deviations from Cobb-Douglas production. For instance, positive values for  $f$  (such as overhead inputs), or negative for  $g$ , would imply marginal revenue exceeds average revenue per input. For simplicity, we treat the impact of measurement error in inputs as common across different inputs (capital, labor, intermediates) here.<sup>13</sup>

In the setting of Section 3, profit maximization by each plant implies

$$\text{TFPR}_i \equiv \frac{\hat{R}_i}{\hat{I}_i} \propto \tau_i \left( \frac{\hat{R}_i}{R_i} \frac{I_i}{\hat{I}_i} \right). \quad (31)$$

Absent measurement error, a plant's TFPR provides a measure of its distortion  $\tau$ . But, to the extent revenue is overstated or inputs are understated, TFPR will overstate  $\tau$ . In that circumstance, the plant's marginal revenue product is less than implied by its TFPR.

The growth rate of a plant's TFPR will reflect the growth rate of its measurement error as well as the growth rate of its  $\tau$ :

$$\Delta \text{TFPR}_i = \Delta \tau_i + \Delta \left( \frac{\hat{R}_i}{R_i} \right) - \Delta \left( \frac{\hat{I}_i}{I_i} \right). \quad (32)$$

$\Delta$  denotes the growth rate of a plant variable relative to the mean in its sector.

If there are only additive measurement errors, then TFPR growth is

$$\Delta \text{TFPR}_i \approx \frac{\Delta \tau_i}{\hat{R}_i/R_i} - \left( \frac{\hat{R}_i - R_i}{\hat{R}_i} - \frac{\hat{I}_i - I_i}{\hat{I}_i} \right) \Delta I_i + \frac{dg_i}{\hat{R}_i} - \frac{df_i}{\hat{I}_i}, \quad (33)$$

where the approximately equals reflects ignoring higher-order terms. As above,  $dx$  denotes the level change in  $x$ , as opposed to  $\Delta x$ , which denotes its percentage change. The response of  $\text{TFPR}_i$  to inputs speaks to the size of additive measurement error in revenue versus that in inputs. TFPR decreases when inputs rise if revenue is overstated relative to inputs ( $\frac{\hat{R}-R}{\hat{R}} > \frac{\hat{I}-I}{\hat{I}}$ ), and TFPR increases when inputs rise when the reverse is true. Because relative measurement error,  $\frac{\hat{R}-R}{\hat{R}}$  versus  $\frac{\hat{I}-I}{\hat{I}}$ , causes  $\text{TFPR}_i$  to mismeasure  $\tau$ , the response of TFPR to inputs can identify the role of such errors in observed TFPR.

By contrast, if there are only multiplicative measurement errors, then the percentage change in TFPR equals:

$$\Delta \text{TFPR}_i = \Delta \tau_i + \Delta \chi_i - \Delta \phi_i. \quad (34)$$

Here TFPR growth provides no information on measurement error in the level of TFPR, except to the extent  $\Delta \tau$ ,  $\Delta \chi$ , and  $\Delta \phi$  project onto those errors. With proportional measurement errors, any increase in true inputs or revenue at a plant will scale up its measurement errors. Here errors that plague TFPR also contaminate the change in revenue relative to the change in inputs.

Going forward, we focus on purely additive measurement error. For this reason, our estimates should be viewed as a conservative assessment of the role of measurement error in generating differences in TFPR. We allow the variance of shocks to measurement error to scale with a plant's productivity  $A$  and distortion  $\tau$ ; larger plants have a larger average absolute value of measurement error. For this reason, we do not predict that measurement errors become less important with trend growth or systematically differ for large and small plants. We find that even this conservative assessment dramatically reduces the size and volatility of inferred misallocation. We further assume that measurement errors are mean zero. Finally, we assume that measurement errors are uncorrelated with the distortion  $\tau$  across plants.

We next show that the relation between a plant's TFPR level and how its revenue growth responds to input growth can address the role of measurement error in TFPR. We then present results for both U.S. and Indian manufacturing.

## 5.2. Identifying measurement error

Our focal point is the elasticity of measured revenue with respect to measured inputs, conditional on plant TFPR taking a particular value—call it  $\text{TFPR}_k$ :

$$\beta_k \equiv \frac{\text{Cov}_k((\Delta \hat{R}_i, \Delta \hat{I}_i))}{\text{Var}_k((\Delta \hat{I}_i))}. \quad (35)$$

For exposition we first assume no measurement error, then allow for errors in both revenue and inputs. Absent measurement error, changes in revenue and inputs simply reflect changes in the plant's productivity and distortion:

$$\Delta \hat{I}_i = \Delta I_i = (\epsilon - 1) \Delta A_i - \epsilon \Delta \tau_i, \quad (36)$$

<sup>13</sup> We do allow and incorporate  $\tau$ 's specific to inputs, but not measurement error specific to inputs. In a previous working paper version, we allowed measurement error specific to each input and it did not affect the results much. The dominant source of measurement error we infer is to all inputs or revenue. This would be consistent with additive measurement error in the form of missed or double-counted sources of revenue or inputs.

$$\Delta \hat{R}_i = \Delta R_i = (\epsilon - 1)(\Delta A_i - \Delta \tau_i). \quad (37)$$

So  $\beta_k$  is given by:

$$\beta_k = 1 + \phi_k, \quad (38)$$

$$\text{where } \phi_k \equiv \frac{\text{Cov}_k((\Delta \tau_i, \Delta I_i))}{\text{Var}_k((\Delta I_i))} = \frac{-\epsilon \cdot \text{Var}_k((\Delta \tau_i)) + (\epsilon - 1) \cdot \text{Cov}_k((\Delta \tau_i, \Delta A_i))}{\text{Var}_k((\Delta I_i))}. \quad (39)$$

$\phi_k$  is the elasticity of  $\Delta \tau$  with respect to  $\Delta I$ .

$\beta_k$  reflects a standard inference problem: a given increase in inputs creates a larger response in revenue if it is driven by  $A$  than if it is driven by a decline in  $\tau$ . If  $\text{Var}_k(\Delta \tau) = 0$  then  $\beta_k = 1$ , whereas if  $\text{Var}_k(\Delta A) = 0$  then  $\beta_k = \frac{\epsilon-1}{\epsilon} < 1$ . If  $\tau$  follows a random walk so that  $\Delta \tau$  is i.i.d., then  $\beta_k$  reduces to  $1 + \phi$  regardless of TFPR. For stationary  $\tau$ , its conditional volatility is greater at extreme  $\tau$ 's, reflecting  $\tau$ 's regression back to its mean. Thus the  $\text{Var}_k((\Delta \tau))$  is greater at extremes for TFPR, implying smaller values for  $\beta_k$ .

With measurement error in plant revenues and inputs, (38) becomes:

$$\beta_k \approx E_k\left(\frac{R_i \hat{I}_i}{\hat{R}_i \hat{I}_i}\right)((1 + \phi_k)) + \psi_k, \quad (40)$$

$$\text{where } \phi_k \equiv \frac{\text{Cov}_k\left(\frac{I_i}{\hat{I}_i} \Delta \tau_i - \frac{df_i}{\hat{I}_i}, \Delta \hat{I}_i\right)}{\text{Var}_k(\Delta \hat{I}_i)} \quad \text{and} \quad (41)$$

$$\begin{aligned} \psi_k \equiv \frac{1}{\text{Var}_k(\Delta \hat{I}_i)} & \left( \text{Cov}_k\left(\frac{dg_i}{\hat{R}_i}, \Delta \hat{I}_i\right) + \text{Cov}_k\left(\frac{R_i \hat{I}_i}{\hat{R}_i \hat{I}_i}, \Delta \hat{I}_i \left(\Delta \hat{I}_i + \frac{I_i}{\hat{I}_i} \Delta \tau - \frac{df_i}{\hat{I}_i}\right)\right) \right. \\ & \left. - E_k(\Delta \hat{I}_i) \text{Cov}_k\left(\frac{R_i \hat{I}_i}{\hat{R}_i \hat{I}_i}, \left(\Delta \hat{I}_i + \frac{I_i}{\hat{I}_i} \Delta \tau - \frac{df_i}{\hat{I}_i}\right)\right) \right). \end{aligned} \quad (42)$$

The approximate equality in (40) means it is a good approximation for relatively small changes in  $A$ ,  $\tau$ ,  $f$ , and  $g$ .

Comparing (38) and (40), with measurement error the factor  $1 + \phi_k$  in  $\beta_k$  scales by  $E_k((\frac{R\hat{I}}{\hat{R}\hat{I}}))$ . If revenue is overstated, then any implied increase in revenue is only manifested to the proportion  $R/\hat{R}$ . If inputs are overstated, then any true increase in inputs is scaled down by  $\hat{I}/I$ , so the response in revenues is scaled up by  $\hat{I}/I$ . The same factor  $\frac{R\hat{I}}{\hat{R}\hat{I}}$  confounds TFPR as a measure of the true distortion  $\tau$ , with the expectation of  $\tau$  at a particular TFPR level  $k$  given by:

$$E_k(\tau_i) = E_k\left(\frac{R_i \hat{I}_i}{\hat{R}_i \hat{I}_i}\right) \cdot \text{TFPR}_k. \quad (43)$$

Using the definition of  $\beta_k$  from (40), we have:

$$E_k(\tau_i) = E_k\left(\frac{R_i \hat{I}_i}{\hat{R}_i \hat{I}_i}\right) \cdot \text{TFPR}_k = \left(\frac{\beta_k - \psi_k}{1 + \phi_k}\right) \cdot \text{TFPR}_k. \quad (44)$$

Measurement error affects the interpretation of  $\phi_k$  and potentially introduces the factor  $\psi_k$ .  $\phi_k$  still reflects the inference problem that the elasticity of measured revenue with respect to measured inputs depends on the source of the change in inputs. There are now three sources of change:  $\Delta A$ ,  $\Delta \tau$  and  $df$ . Increases in measured inputs driven either by a decrease in  $\tau$  or an increase in  $f$  result in smaller responses in revenue than do increases in  $A$ . Turning to  $\psi_k$ , its first element allows for the possibility that changes in measurement errors in revenue are correlated with measured changes in inputs. The latter terms are more subtle, reflecting any correlations between the measurement error component of TFPR, in levels, and changes in inputs or measurement errors.

If  $\Delta \tau$ ,  $\Delta A$ ,  $df/\hat{I}$  and  $dg/\hat{R}$  are each i.i.d., then  $\psi_k = 0$  and  $\phi_k$  reduces to  $\phi$ , independent of the level of TFPR. In this case  $\beta_k \approx E_k((\frac{R\hat{I}}{\hat{R}\hat{I}}))((1 + \phi))$  and (44) yields:

$$E_k(\tau_i) \propto \beta_k \cdot \text{TFPR}_k. \quad (45)$$

Thus, given estimates of the  $\beta_k$ 's, we can answer the question: If two plants differ in TFPR, what is the expected difference in their actual marginal revenue products due to differences in their  $\tau$ 's. If differences in TFPR partially reflect errors  $f$  or  $g$ , then  $\hat{\beta}_k$ 's will be systematically lower at higher TFPR's.

We will use equation (45) as a benchmark to correct TFPR for measurement error. In general,  $\psi_k \neq 0$  and  $\phi_k$  will depend on the level of lagged TFPR. To address these possibilities, we will simulate a model economy under plausible scenarios

to see if our simple correction using (45) overstates or understates the role of measurement error in TFPR dispersion. In particular, we will simulate models where  $\Delta\tau$ ,  $\Delta A$ ,  $\frac{df}{f}$  and  $\frac{dg}{g}$  are not i.i.d., for instance due to  $\tau$ ,  $A$ , or measurement errors being stationary. To anticipate, we will find that our correction based on (45) is quite accurate for a wide range of parameter values, especially if measurement errors are only moderately large. For very large measurement errors, we find (45) tends to *under* estimate the role of measurement error, rendering our corrections somewhat conservative.

From (45), we can capture the dispersion in  $\tau$ 's that is predicted by TFPR's. But in the presence of measurement error there will also be differences in  $\tau$ 's that are orthogonal to TFPR. For instance, a plant with a high value for  $\tau$  but understated revenue might display purely average TFPR. To capture this component, we “add back” variation in  $\tau$ 's that is orthogonal to TFPR, under an assumption that true  $\tau$  is orthogonal to the measurement error component of TFPR.

From the relation between TFPR,  $\tau$ , and measurement error, we have:

$$\text{Var}\left(\ln \tau_i\right) = \text{Var}\left(\ln \text{TFPR}_i\right) - \text{Var}\left(\ln \left(\frac{R_i \hat{I}_i}{\hat{R}_i I_i}\right)\right) + 2 \text{Cov}\left(\ln \tau_i, \ln \left(\frac{R_i \hat{I}_i}{\hat{R}_i I_i}\right)\right). \quad (46)$$

We assume that the two components of TFPR, namely the true distortion  $\tau$  and the measurement error component  $\frac{\hat{R}I}{RI}$ , are orthogonal to each other in their natural logs. This eliminates the last term in equation (46). Furthermore, the middle term can be written as the two terms:<sup>14</sup>

$$-\text{Var}\left(\ln \left(\frac{R_i \hat{I}_i}{\hat{R}_i I_i}\right)\right) = \text{Cov}\left(\ln \text{TFPR}_k, E_k\left(\ln \left(\frac{R_i \hat{I}_i}{\hat{R}_i I_i}\right)\right)\right) - \text{Cov}\left(\ln \tau_i, \ln \left(\frac{R_i \hat{I}_i}{\hat{R}_i I_i}\right)\right), \quad (47)$$

which reduces to its first term, given the assumption  $\tau$  and  $\frac{\hat{R}I}{RI}$  are orthogonal.

Thus equation (46) can be reduced to:

$$\text{Var}\left(\ln \tau_i\right) = \text{Var}\left(\ln \text{TFPR}_i\right) + \text{Cov}\left(\ln \text{TFPR}_k, E_k\left(\ln \left(\frac{R_i \hat{I}_i}{\hat{R}_i I_i}\right)\right)\right). \quad (48)$$

The first term is data. The second is provided by how the estimates of  $\beta_k$ , discussed earlier in this subsection, covary with TFPR. We add back dispersion in  $\tau$  that is mean zero and orthogonal to TFPR, with variance dictated by equation (48). In turn, that variance can be expressed as:

$$\sigma^2 = -\text{Cov}\left(\ln(\text{TFPR}_k), \ln\left(\frac{\beta_k - \psi_k}{1 + \phi_k}\right)\right) - \text{Var}\left(\ln\left(\frac{\beta_k - \psi_k}{1 + \phi_k}\right)\right). \quad (49)$$

We assume this component in  $\tau$ , orthogonal to TFPR, is distributed lognormally.

### 5.3. Recapping our approach

To recap, our procedure takes the following steps:

1. For a sample of panel plants, construct output growth, composite input growth and deciles of TFPR (Tornqvist deviations from sector-year average).
2. Regress output growth on input growth separately for each decile  $k$  of TFPR, weighted by each plant's share of aggregate costs. The coefficients on input growth are the estimates  $\hat{\beta}_k$ .
3. Merge  $\hat{\beta}_k$  estimates into the full cross-sectional dataset of plants using the cutoffs between each TFPR decile from the panel estimation.
4. Construct corrected variance of  $\ln(\text{TFPR})$  to equal the variance of  $\ln(\text{TFPR})$  plus the covariance of  $\ln(\text{TFPR})$  and  $\ln(\hat{\beta}_k)$ .
5. Correct misallocation from plant-level  $\hat{\tau}$  estimates, constructed as  $\ln(\hat{\tau}) = \ln(\text{TFPR}) + \ln(\hat{\beta}_k) + \varepsilon$ , for  $\varepsilon$  distributed log-normal with mean zero and variance equal to:  $-\text{Cov}[\ln(\text{TFPR}), \ln(\hat{\beta}_k)] - \text{Var}(\ln(\hat{\beta}_k))$ .

The intuition for our approach is as follows. Absent measurement errors, the elasticity of plant revenue with respect to inputs  $\beta$  should not depend on a plant's level of TFPR. As outlined in Section 5.2, while  $\beta$  will generally be less than one, unless the relative volatility of shocks to firm  $\tau$ 's are correlated with the level of TFPR, then TFPR does not predict  $\beta$ . By contrast, under additive measurement errors, measurement error maps to a lower elasticity  $\beta$ . Therefore, the relation of  $\hat{\beta}$  to TFPR speaks to the role of measurement error in TFPR dispersion, in turn yielding an expected true distortion  $\tau$  for a plant, given its TFPR. Furthermore, we can correct allocative efficiency for the role of the measurement errors, conditional on a covariance of measurement error with true distortions. We do so for the case of zero covariance in Section 7.

<sup>14</sup> This step uses that  $\ln\left(\frac{\hat{R}I}{RI}\right)$  equals  $(-\ln \text{TFPR} + \ln \tau)$  and that it can also be broken into  $E_k\left(\ln\left(\frac{\hat{R}I}{RI}\right)\right)$  and  $\left(\ln\left(\frac{\hat{R}I}{RI}\right) - E_k\left(\ln\left(\frac{\hat{R}I}{RI}\right)\right)\right)$ .

**Table 1**  
Coefficients  $\hat{\beta}_k$  for revenue growth on input growth by TFPR decile.

Decile $k \rightarrow$	1	2	3	4	5	6	7	8	9	10
India	1.087	1.040	1.027	0.996	1.007	0.991	0.996	0.989	0.951	0.882
1985–2013	(.017)	(.012)	(.010)	(.014)	(.011)	(.011)	(.009)	(.014)	(.010)	(.011)
U.S.	1.046	0.995	0.969	0.961	0.931	0.896	0.863	0.837	0.704	0.541
1978–2013	(.013)	(.019)	(.015)	(.019)	(.020)	(.016)	(.014)	(.019)	(.021)	(.021)

Source: Indian ASI and U.S. LRD. Entries are coefficients from regressing revenue growth on input growth by decile of  $\ln(\text{TFPR})$ , as shown in [equation \(50\)](#). TFPR deciles are constructed as Tornqvist deviations from the (cost-weighted) sector-year average. Decile 1 corresponds to the lowest decile of TFPR, and Decile 10 the highest decile of TFPR. Regressions are weighted by each plant's (Tornqvist) share of all input costs. Standard errors are clustered at the industry level. There are 1,423,000 plant growth rate observations in the U.S. sample, and 318,311 observations in the India sample.

#### 5.4. Estimates for India and the U.S.

For both India and the U.S. we start with plants that are observed in consecutive years. This reduces the number of observations in the U.S. to 1,423,000 and in India to 318,311. We then divide each country's data into separate time windows. For India we have growth rates for 1985–1986 to 2013–2014 that we split into five windows of approximately six years each.<sup>15</sup> For the U.S. we divide 36 years in growth rates from 1978–1979 to 2013–2014 into five windows of approximately seven years each. We then regress plant revenue growth on plant input growth by decile of TFPR in each window:

$$\Delta \hat{R}_i = \hat{\lambda}_k + \hat{\beta}_k \Delta \hat{I}_i + e_i, \quad (50)$$

Here  $i$  denotes the plant and  $k$  the decile of TFPR.  $\Delta \hat{R}_i$ ,  $\Delta \hat{I}_i$  and TFPR are each deviations from the sector-year average for that plant. The individual decile-windows contain on average 13,000 plants per year for India and 41,000 for the U.S. Within each decile, plants are weighted by their share of total input costs.<sup>16</sup>

Measurement error is manifested in a lower  $\beta$  at higher levels of TFPR. We first report  $\hat{\beta}$  by decile of TFPR, pooling all years for each country. The estimates are in [Table 1](#). Looking first at India, we see a clear tendency for  $\hat{\beta}$  to decline with the level of TFPR. This decline is most pronounced in the top two deciles of TFPR. The difference in  $\hat{\beta}$  going from the bottom to the top decile is  $-0.205$  with a standard error of  $0.020$ .<sup>17</sup> For the U.S. the negative relationship between TFPR and  $\hat{\beta}$  is even more striking.  $\hat{\beta}$  declines monotonically with TFPR and, as in India, most sharply in the top two deciles of TFPR. The difference in  $\hat{\beta}$  between the top and bottom deciles is  $-0.505$  with a standard error  $0.025$ .<sup>18</sup>

How does the relation between TFPR and  $\hat{\beta}$  change through time? [Fig. 3](#) displays these estimates for India and the U.S., with  $\ln(\hat{\beta})$  plotted against  $\ln(\text{TFPR})$  by sample period. For India,  $\hat{\beta}$  decreases with TFPR to a similar degree in all periods. [Fig. 3](#) reveals the increase in U.S. TFPR dispersion over time, manifested by the increasing spread with respect to TFPR in later periods. Over time  $\hat{\beta}$  becomes much more negatively related to TFPR in the United States. Thus the increased dispersion in TFPR in the U.S. is associated with an increased role for measurement error in that dispersion.

Given the  $\hat{\beta}_k$  estimates, we construct a corrected cross-sectional distribution of distortions  $\tau$ 's for each time frame in each country according to:

$$\ln(\hat{\tau}) = \ln(\text{TFPR}) + \ln(\hat{\beta}_k) + \varepsilon. \quad (51)$$

More exactly, each plant in a cross-sectional sample is assigned the  $\hat{\beta}_k$  estimated for the TFPR decile corresponding to its TFPR.<sup>19</sup>  $\varepsilon$  is drawn from a log normal distribution, conditional on TFPR, with variance as dictated by [equation \(49\)](#).<sup>20</sup>

We report the resulting dispersion in  $\ln(\tau)$ 's over time for each country in [Table 2](#), expressed in terms of the variance of  $\ln(\hat{\tau})$  relative to the variance of  $\ln(\text{TFPR})$ . For India, the variance of  $\hat{\tau}$  is consistently about 30% smaller than the variance of TFPR. For the U.S. we estimate an even bigger and growing role for measurement error. In the U.S. the variance of  $\hat{\tau}$  is about 70% lower than that for TFPR from 1999 onward. The implication, we shall see, is that measurement error exaggerates

<sup>15</sup> Because of breaks in the panel identifiers, we have growth rates for only 25 of the 29 years.

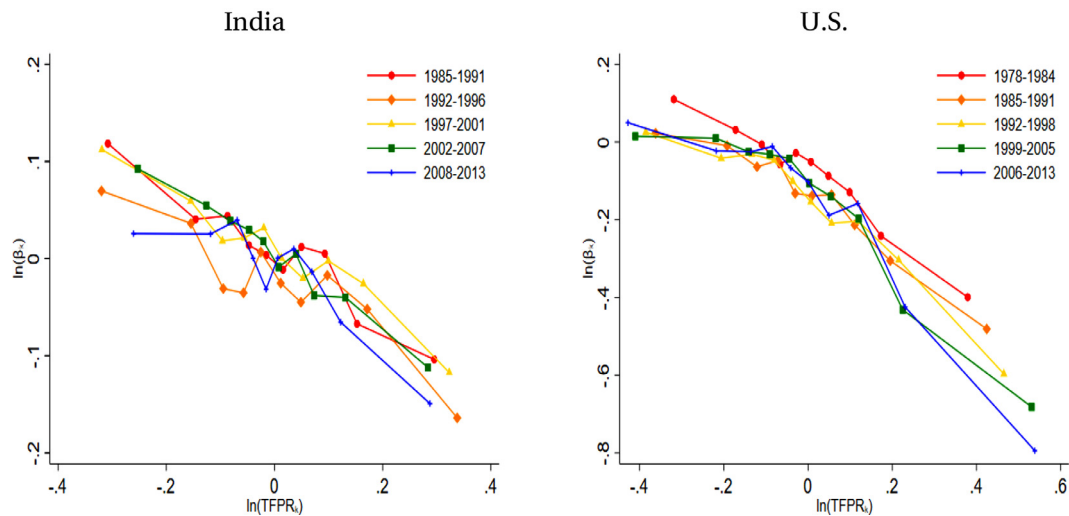
<sup>16</sup> More precisely, a plant's share of inputs reflects the (Tornqvist) average of its shares across the annual observations being differenced. Similarly, a plant's relative TFPR reflects the average of its relative TFPRs across the two years. In constructing a plant's input growth rate, growth rates in intermediates, labor, and capital are weighted by its sector's average input shares. Observations where TFPR increases or decreases by a factor greater than five are excluded.

<sup>17</sup> We cluster our standard errors at the industry level. Our standard errors are approximately one third smaller if we cluster at the plant level.

<sup>18</sup> Figures A8 and A9 in our [Online Appendix](#) split the samples by plant size and age, respectively. We find evidence that measurement error is more severe among larger firms in both the U.S. and India. Measurement error appears worse for older firms in the U.S., but for younger firms in India.

<sup>19</sup> Some years in the cross-sectional sample appear in two separate windows. For instance the year 2002 for India is spanned by the panel window covering growth rates from 1997–1998 to 2001–2002 as well as the window for growth rates from 2002–2003 to 2007–2008. For such years we average the  $\hat{\beta}$ 's for its backward and forward-looking windows.

<sup>20</sup> Comparing [equations \(51\)](#) and [\(45\)](#), we have replaced  $\ln(E_k(\tau))$  with  $E_k(\ln(\tau))$ . For  $\ln(\tau)$  conditionally distributed lognormal, this adds a sector-specific constant term that does not enter into measured dispersion.



**Fig. 3.** India and U.S.  $\beta$  Slopes Source: Indian ASI and U.S. LRD. The figures plot the  $\hat{\beta}_k$  coefficients recovered from running the regressions in (50) against deciles of TFPR. In each time window and for each TFPR decile  $k$ , revenue growth is regressed on input growth to obtain  $\hat{\beta}_k$ . The relationship is plotted separately for five different time windows.

**Table 2**  
Dispersion in Marginal Products vs. TFPR Dispersion.

Panel A: India					
	1985–1991	1992–1996	1997–2001	2002–2007	2008–2013
$\frac{\sigma_{\hat{\tau}}^2}{\sigma_{\text{TFPR}}^2}$	0.739	0.763	0.745	0.697	0.732
Panel B: U.S.					
	1978–1984	1985–1991	1992–1998	1999–2005	2006–2013
$\frac{\sigma_{\hat{\tau}}^2}{\sigma_{\text{TFPR}}^2}$	0.404	0.432	0.379	0.325	0.274

Source: Indian ASI and U.S. LRD. The table shows the ratio of the variance of  $\ln(\hat{\tau})$  to the variance of  $\ln(\text{TFPR})$ , for both India and the U.S. for five different time periods. Variances are output share weighted.  $\hat{\tau}$  is constructed as in equation (51).

misallocation in both countries, but especially in the U.S. in recent years.<sup>21</sup> But first, in the next section, we use simulations of a wider range of models to examine the robustness of our approach.

## 6. How robust is our approach?

Our derivations simplified the analysis by assuming i.i.d. shocks to the growth rates of productivity,  $\tau$ 's, and measurement errors. More generally, the expectation of  $\hat{\beta}$  depends on the expected importance of shocks to productivity,  $\tau$ 's, and measurement errors. Because TFPR reflects  $\tau$  and measurement errors, this allows an additional channel for  $\hat{\beta}$  to differ across the distribution of firm TFPRs.<sup>22</sup> For this reason, we now explore the robustness of our approach in a simulated economy without i.i.d. shocks. Furthermore, the simulations show how the procedure performs for realistically-sized shocks, realistic in that they align with the targeted empirical moments. This is useful since our derivations make use of first-order approximations. We match simulated moments to data moments for India and the United State. We find that our estimator

<sup>21</sup> Our estimated variance for  $\ln(\tau)$ , which underlies our measure of allocative efficiency, is given by  $\widehat{\text{Var}}[\ln(\tau)] = \widehat{\text{Var}}[\ln(\text{TFPR})] + \widehat{\text{Cov}}[\ln(\text{TFPR}), \ln(\beta)]$ . There are two elements of sampling error in this estimate. The first is that  $\widehat{\text{Var}}[\ln(\text{TFPR})]$  may differ from its population moment. But given the large sample sizes we employ for both the U.S. and India, this generates standard errors that are a couple order of magnitudes smaller than our estimated variances for  $\ln(\tau)$ . For instance, if  $\ln(\text{TFPR})$  is distributed normally, the standard error for  $\widehat{\text{Var}}[\ln(\text{TFPR})]$  would be only about 1/150 of our estimated variance for  $\ln(\tau)$  for both India and the United States. A more important source of error arises from uncertainty in our measure of  $\widehat{\text{Cov}}[\ln(\text{TFPR}), \ln(\beta)]$  reflecting uncertainty in our estimates for  $\beta$ . To assess its magnitude, for each country we construct the  $\widehat{\text{Cov}}[\ln(\text{TFPR}), \ln(\beta)]$  across TFPR deciles for each of 100 separate draws of  $\hat{\beta}$ 's, each independently drawn from a normal distribution with mean and standard deviation dictated by the point estimates and standard errors for that country's  $\hat{\beta}$ 's. (Each draw actually implies 10 distinct draws, one for each decile of TFPR. For India the sample pools years, 1985–2013, for the U.S. 1978–2013.) The distribution of those estimated covariances imply a standard error for  $\widehat{\text{Cov}}[\ln(\text{TFPR}), \ln(\beta)]$  of 0.0007 for India and 0.0022 for the United States. These are more significant than the sampling error in  $\widehat{\text{Var}}[\ln(\text{TFPR})]$ . But they still imply standard errors for  $\widehat{\text{Var}}[\ln(\tau)]$  that are relatively small, by at least an order of magnitude, compared to our estimated  $\widehat{\text{Var}}[\ln(\tau)]$  for each country.

<sup>22</sup> This gives rise to the terms  $\phi_k$  and  $\psi_k$  in  $\beta_k$  discussed in Section 5.2.

performs well even if measurement error is sizable, such as we estimate for India. If measurement error is enormously important, as we find for the U.S., then our approach is conservative, as it tends to understate the role of measurement error in TFPR dispersion.

### 6.1. Simulations

We assume that plant  $i$ 's idiosyncratic productivity in period  $t$  is given by:

$$A_{it} = A_i \cdot a_{it}. \quad (52)$$

$A_i$  is the permanent component of a plant's productivity, which we assume is lognormally distributed:  $\ln(A_i) \sim N(0, \sigma_A^2)$ .  $a_{it}$  is the transitory component of plant productivity. Plants also face an idiosyncratic, time-varying distortion  $\tau_{it}$ .  $a_{it}$  and  $\tau_{it}$  follow:

$$\ln(a_{it}) = \rho_a \cdot \ln(a_{it-1}) + \eta_{it}^a \text{ where } \eta_{it}^a \sim N(0, \sigma_a^2), \quad (53)$$

$$\ln(\tau_{it}) = \rho_\tau \cdot \ln(\tau_{it-1}) + \eta_{it}^\tau \text{ where } \eta_{it}^\tau \sim N(0, \sigma_\tau^2). \quad (54)$$

Measurement errors in inputs and revenues follow AR(1) processes, with the variance of the shocks scaling with the size of the plant:

$$f_{it} = \rho_f \cdot f_{it-1} + \eta_{it}^f \cdot I_{it} \text{ where } \eta_{it}^f \sim N(0, \sigma_f^2), \quad (55)$$

$$g_{it} = \rho_g \cdot g_{it-1} + \eta_{it}^g \cdot R_{it} \text{ where } \eta_{it}^g \sim N(0, \sigma_g^2). \quad (56)$$

As a baseline, we consider the case with measurement error in inputs only. We set  $\epsilon = 4$  and  $\rho_a = \rho_\tau = \rho_f = 0.9$  and use the simulated method of moments (simulating 30,000 plants over 50 years) to calibrate  $\sigma_\tau$ ,  $\sigma_A$ ,  $\sigma_a$  and  $\sigma_f$ .<sup>23</sup> We target four moments from the data: the (output share weighted) variance of  $\ln(\text{TFPR})$ , the unweighted variance of  $\ln(\text{TFPQ})$ , the slope of  $\ln(\hat{\beta})$  vs. Tornqvist  $\ln(\text{TFPR})$  across deciles, and the variance of input growth.<sup>24</sup>

The parameters are jointly calibrated, but they are differentially important for certain moments. The variance of  $\ln(\text{TFPR})$  and the  $\ln(\hat{\beta})$  slope are particularly important in disciplining the values of  $\sigma_\tau$  and  $\sigma_f$ . The variance of  $\ln(\text{TFPQ})$  is sensitive to the variance of the permanent component of firm productivity  $\sigma_A$ , while the variance of input growth relates strongly to the variance of productivity shocks  $\sigma_a$ . Table 3 shows our estimated parameter values. The targeted data moments and simulated moments for each time period in India and the U.S. are provided in Table A2 in our Online Appendix. The simulated moments are always close to the targeted moments – though not exactly the same because the relationship between parameters and moments is non-linear.

The main outcome of interest is how accurately our estimator captures the variance of distortions relative to TFPR dispersion,  $\sigma_\tau^2 / \sigma_{\text{TFPR}}^2$ . Given that  $\tau$  and  $A$  are lognormally distributed in the model, the variance of  $\sigma_\tau^2$  is proportional to allocative efficiency. We compare our estimated share  $\sigma_\tau^2 / \sigma_{\text{TFPR}}^2$  to the true share for India and the U.S. in Table 4. Our estimator performs remarkably well for India in all time periods. While conservative, in that it understates the role of measurement error, it deviates from the true share of distortions in TFPR dispersion by less than 1.3 percentage points on average. For the U.S. the discrepancy is larger. We overestimate the share of true distortions in TFPR dispersion for all periods, particularly when there is a lot of measurement error. For the 2006–2013 window, our estimator says the variance of distortions is one fourth the variance of TFPR, when in fact it is only one fiftieth. Despite this, our estimator does capture reasonably well the movements over time in the share of distortions in TFPR dispersion.

We obtain similar results when we add the autocorrelation of log TFPR as a targeted moment, with  $\rho = \rho_\tau = \rho_f$  as an additional parameter. Likewise, we obtain similar results if measurement error is in revenues rather than inputs. Although we have more difficulty simultaneously hitting all targeted data moments, our estimator continues to be a conservative gauge of the importance of measurement error. We provide these results in our Online Appendix.

In our Online Appendix we also check how multiplicative measurement error and adjustment costs affect our estimator. As expected, if all measurement error is multiplicative we find that our estimator predicts that TFPR dispersion stems entirely from distortions. So, in the presence of multiplicative errors, our estimated share of measurement error in TFPR dispersion is conservative. We also consider a model with adjustment costs whereby a plant chooses its inputs one period ahead, before its productivity shock is observed. Our estimator interprets TFPR dispersion due to adjustment costs as if this dispersion was due to true distortions. This would suggest that, if adjustment costs are important in the U.S. and India, the share of TFPR dispersion due to  $\tau$  dispersion may be even lower than what our estimator finds.

<sup>23</sup> We clean the simulated data in the same way we do the actual micro data: dropping observations with negative revenues or inputs and those where TFPR changes by a factor of five or more. We simulate all plants for 50 years, and then construct the simulated moments as the average value over the last 30 years.

<sup>24</sup> We minimize the sum of the absolute log differences between the targeted data moments and the simulated moments.

**Table 3**  
Calibrated Parameter Values.

	$\sigma_\tau$	$\sigma_A$	$\sigma_a$	$\sigma_f$
Panel A: India				
1985–1991	0.060	0.637	0.181	0.030
1992–1996	0.074	0.711	0.102	0.040
1997–2001	0.073	0.712	0.088	0.042
2002–2007	0.056	0.733	0.110	0.039
2008–2013	0.060	0.744	0.113	0.035
Panel B: U.S.				
1978–1984	0.036	0.520	0.103	0.079
1985–1991	0.053	0.517	0.075	0.088
1992–1998	0.050	0.542	0.071	0.103
1999–2005	0.044	0.500	0.070	0.123
2006–2013	0.017	0.494	0.103	0.130

Source: This table shows the parameter values recovered from the model calibration. The model is calibrated for both India and the U.S. separately for five different time periods.  $\sigma_\tau$  is the standard deviation of the shocks to the distortions,  $\sigma_A$  is the standard deviation of the permanent component of plant productivity,  $\sigma_a$  is the standard deviation of the time-varying component of plant productivity, and  $\sigma_f$  is the standard deviation of shocks to measurement error in inputs.

**Table 4**  
Simulations: Our Estimator vs. Truth.

Panel A: India					
	1985–1991	1992–1996	1997–2001	2002–2007	2008–2013
$\frac{\sigma_\tau^2}{\sigma_{TFPR}^2}$ (our estimator)	0.678	0.712	0.699	0.640	0.692
$\frac{\sigma_\tau^2}{\sigma_{TFPR}^2}$ (truth)	0.604	0.693	0.682	0.581	0.656
Panel B: U.S.					
	1978–1984	1985–1991	1992–1998	1999–2005	2006–2013
$\frac{\sigma_\tau^2}{\sigma_{TFPR}^2}$ (our estimator)	0.334	0.407	0.366	0.304	0.236
$\frac{\sigma_\tau^2}{\sigma_{TFPR}^2}$ (truth)	0.143	0.240	0.181	0.107	0.015

Source: This table shows, for simulated data, the ratio of the variance  $\ln(\hat{\tau})$  to the variance of  $\ln(TFPR)$ , and the ratio of the true variance of  $\ln(\tau)$  to the variance of  $\ln(TFPR)$ . Results are for both India and the U.S., and for five different time-periods each. The parameters used to generate each of these results are shown in Table 3.

## 7. Revisiting misallocation

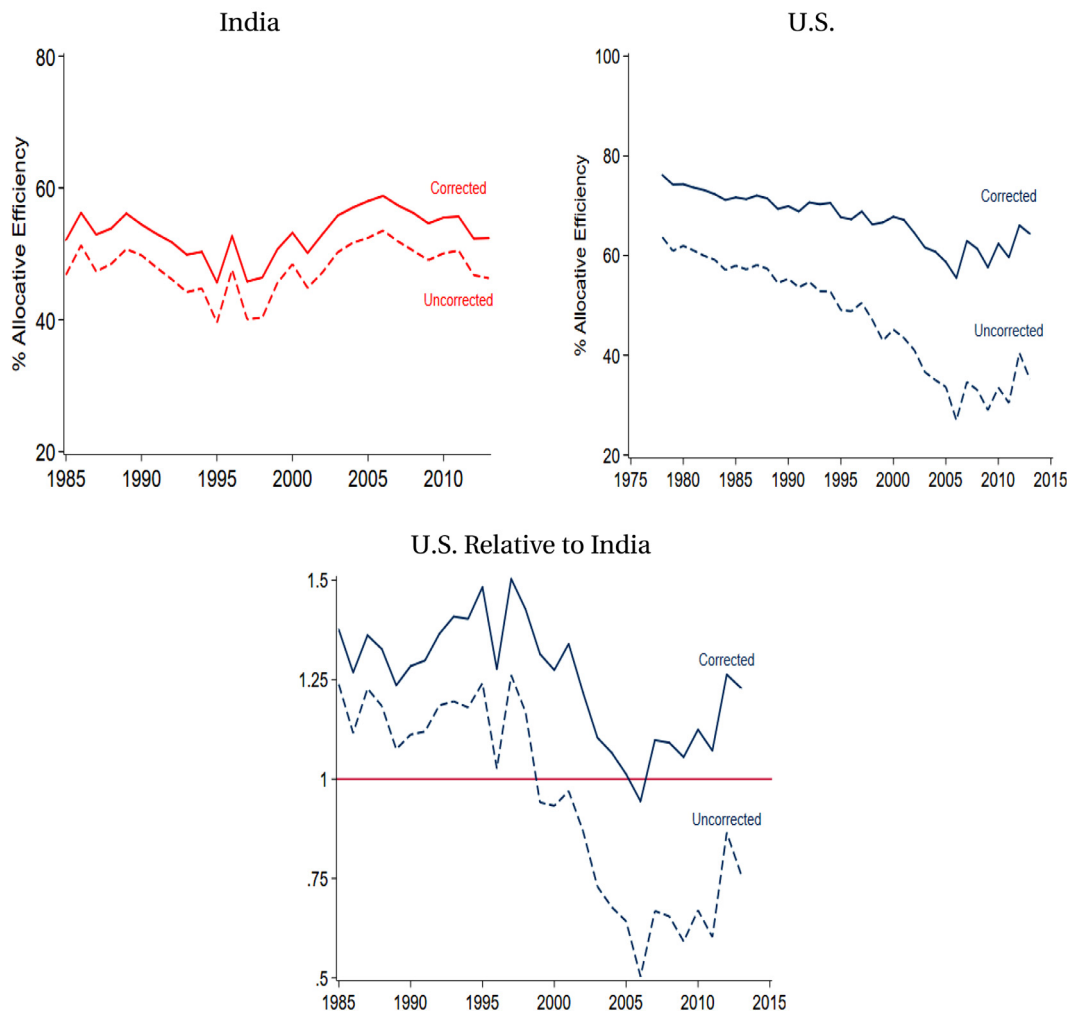
We now compare the “raw” measures of allocative efficiency for Indian and U.S. manufacturing to our estimates purging the impact of measurement error. This is achieved by replacing TFPR as an estimate of  $\tau$  with the estimated dispersion of  $\tau$ 's implied by equation (51), which we repeat here for convenience:

$$\ln(\hat{\tau}) = \ln(TFPR) + \ln(\hat{\beta}_k) + \varepsilon. \quad (57)$$

To construct allocative efficiency we also need measures of plant TFPQ and sectoral TFPR. Measurement error in inputs affects TFPQ and TFPR in the same way; so we get that  $\ln(\hat{A}) = \ln(TFPQ) + \ln(\hat{\beta}_k) + \varepsilon$ .<sup>25</sup> To construct sectoral TFPR we need corrected measures of sectoral MRPL, MRPX and MRPK.<sup>26</sup> We assume that measurement error is common to all inputs, and therefore affects each of these in the same way.<sup>27</sup> Our estimates for  $\ln(\hat{\beta}_k)$  are in Fig. 3.

We display corrected vs. uncorrected allocative efficiency for India in the top left panel of Fig. 4. Averaging across years, the correction increases allocative efficiency modestly from 48% to 53%. The impact of the correction is fairly stable for India across the 29 years. Another way to express misallocation is in terms of the increase in productivity that can be reaped





**Fig. 4.** Corrected Allocative Efficiency Source: Indian ASI and U.S. LRD. The India sub-figure shows uncorrected and corrected allocative efficiency (AE) for years 1985 to 2013. Average uncorrected AE is 47.7% while average corrected AE is 53.4%. The U.S. sub-figure show uncorrected and corrected allocative efficiency (AE) for years 1978 to 2013. Average uncorrected AE is 47.6% while average corrected AE is 67.4%. The bottom figure shows uncorrected and corrected allocative efficiency for the U.S. relative to India for years 1985 to 2013.

by attaining perfect (100%) allocative efficiency. This is reported for India in Table 5. With distortions measured by TFPR dispersion, the potential increase in productivity is 111%. Based on the corrected numbers it is 21 percent lower, at 89%.

In the top right panel of Fig. 4 we see a far greater impact in the United States. Our correction eliminates more than half of potential gains from reallocation and the lion's share of the conspicuous downward trend in allocative efficiency. Allocative efficiency declines by 15% over the 35 years according to our corrected series. While significant, this is only a third of the 45% decline with no corrections.

Table 5 reports the potential percent gains from going to 100% allocative efficiency in the United States. The correction reduces potential gains, averaged across years, from 123 percent down to 49 percent. In addition to dampening the trend in misallocation, the correction moderates its higher frequency vagaries. As a result, volatility for the time series for gains, as measured by its standard deviation, plummets from 60 percent down to 12 percent.

Our corrections dramatically affect comparisons of allocative efficiency in the U.S. versus India. The bottom panel of Fig. 4 displays the allocative efficiency for the U.S. relative to that in India. Without correcting, the U.S. averages a 16 percent advantage in allocative efficiency for the first ten years (1985 to 1994). But in the last ten years, U.S. efficiency collapses

<sup>25</sup> This expression is exact if measurement error contaminates only inputs, which we presume in presenting our results. Measurement error in revenues enters TFPR with amplification  $\frac{\epsilon}{\epsilon-1}$ . But we find this is not quantitatively important under our elasticity of demand of  $\epsilon = 4$ . Hence our results do not hinge on assuming that measurement errors only affect inputs.

<sup>26</sup> Recall that  $TFPR_s = \left(\frac{\epsilon}{\epsilon-1}\right) \left[\frac{MRPL_s}{(1-\alpha_s)^{\gamma_s}}\right]^{(1-\alpha_s)\gamma_s} \left[\frac{MRPK_s}{\alpha_s\gamma_s}\right]^{\alpha_s\gamma_s} \left[\frac{MRPX_s}{1-\gamma_s}\right]^{1-\gamma_s}$

<sup>27</sup> That is,  $\ln(MRPL) = \ln(MRPL) + \ln(\hat{\beta}_k) + \varepsilon$ , and similarly for MRPK and MRPX.

**Table 5**  
Uncorrected and Corrected Gains from Reallocation.

	India		U.S.	
	Mean	S.D.	Mean	S.D.
Uncorrected gains	110.8%	17.1%	123.1%	59.7%
Corrected gains	89.0%	12.9%	49.2%	12.1%
Shrinkage	21%	20%	60%	80%

Source: Indian ASI and U.S. LRD. This table reports the average and standard deviation of uncorrected and corrected gains from improving allocative efficiency to 100% in India (1985–2013) and the U.S. (1978–2013). The shrinkage is the percent reduction in the average or standard deviation of gains after our corrections.

relative to India. Over those years U.S. efficiency averages only two-thirds that for India. Our corrected series, however, looks entirely different. The U.S. advantage relative to India is much higher, averaging 25 percent, compared to - 6 percent uncorrected. The U.S. advantage remains positive throughout, with a modest exception in 2006.

We demonstrated in [Section 4.3](#) that the perceived decline in allocative efficiency for the U.S. mapped directly to a sharp rise in the variance of  $\ln(\text{TFPR})$  in the United States. It should come as no surprise, then, that our correction to allocative efficiency reflects much less estimated dispersion in  $\tau$ 's. We show that this is indeed the case in our [Online Appendix](#). Dispersion in our corrected TFPR series is much lower, trends less, and is generally less volatile.

Our adjustments for measurement error also alter the implied elasticity of TFPR with respect to TFPQ in the United States. As shown in our [Online Appendix](#), our corrections lower the elasticity and its upward drift. [Bento and Restuccia \(2017\)](#) and [Decker et al. \(2020\)](#) highlight this elasticity as indicative of barriers to investing in, or benefiting from, higher TFPQ at the plant level. Related, our corrections undermine the case that TFPQ dispersion has risen across plants in the U.S. (see [Online Appendix](#)), as emphasized for example by [Gouin-Bonenfant \(2019\)](#).

## 8. Conclusion

We proposed a way to estimate the true dispersion of marginal products across plants in the presence of additive measurement errors in revenue and inputs. We showed that the response of revenue *growth* to input *growth* should be lower for high-TFPR plants in the presence of measurement error. We then used the projection of that response on TFPR to correct for measurement error. While our method employs several assumptions, we used simulations to demonstrate that our approach is robust or at least conservative.

We implemented our method on data from the Indian *Annual Survey of Industries* from 1985–2013 and the US. *Annual Survey of Manufacturing* from 1978–2013. In India, we estimated that true marginal products were significantly less dispersed than average products. As a result, potential gains from reallocation fell 21% and the volatility of those gains across years fell by 20%. In the U.S. our correction had even more bite. Average potential gains from reallocation fell by 60%, while time-series volatility fell by 80%. Our correction eliminated 2/3 of a severe downward trend in allocative efficiency for the U.S. Even corrected, allocative efficiency declined by 15% for U.S. manufacturing over the 35 years. Based on uncorrected data, allocative efficiency was 6% *lower* in the U.S. than in India for 1985 to 2013. In contrast, our corrected series implies consistently higher allocative efficiency in the U.S. than in India.

We hope our method provides a useful diagnostic for measurement errors that can be applied when researchers have access to panel data on plants and firms. For example, [David and Venkateswaran \(2019\)](#) and [Bai et al. \(2019\)](#) apply our correction to firm-level data for China.

Our findings leave many open questions for future research. Why did measurement error worsen considerably over time in the U.S.? Why, even after our corrections, does ample misallocation remain in the U.S. and India? Is this real or due to some combination of model misspecification and proportional measurement error? If it is real, can it be traced to specific government policies or market failures (e.g. markup dispersion or capital/labor market frictions)?

## Transparency declaration

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## Supplementary material

Supplementary material associated with this article can be found, in the online version, at doi:[10.1016/j.jmoneco.2021.09.004](https://doi.org/10.1016/j.jmoneco.2021.09.004).

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